

Hydro-sedimentological computational tool: case study of the Mogi-Guaçu SHP (Brazil-SP)

Ferramenta computacional hidrossedimentológica: estudo de caso da PCH de Mogi-Guaçu (Brazil-SP)

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Abstract

The hydro-sedimentological studies are complex and of great importance, mostly in countries with large amounts of water resources and with its energy matrix predominantly hydraulic. The assessment of the amount of sediment carried through water bodies is more difficult mainly due to the amount of involved quantities, which require the adoption of probabilistic or deterministic estimation methods. In this context, this paper presents a case study that applies the hydros-sedimentological module from the computational tool NH Statistic and Sediment, developed by one of the authors, written in Visual Basic for Applications to determine total sediment discharge using data from the Mogi-Guaçu Small Hydro Electric Power Plant (SP-Brazil). Among the surveys, the reduction of total sediment discharge was verified, which was expected. Likewise, the results provided by the developed computational tool were compared to the results of other softwares showing minimal differences, giving validity and consistency to the applied method. It's worth mentioning that the method used in this case study may be replicated in other places, giving more information to assist the water resource management.

Keywords: Hydro-sedimentology; Total sediment discharge; Computational tool; Visual basic for Applications

Resumo

Os estudos hidrossedimentológicos são complexos e de grande importância principalmente em países com grande quantidade de recursos hídricos e com matriz energética predominantemente hidráulica. A determinação da quantidade de sedimento transportada em um corpo hídrico é dificultada principalmente devido à maior quantidade de grandezas intervenientes, o que requer a aplicação de métodos de estimativa probabilísticos ou determinísticos. Nesse contexto, este artigo apresenta um estudo de caso empregando o módulo hidrossedimentológico da ferramenta computacional NH Statistic and Sediment, desenvolvida por um dos autores, com linguagem de programação em Visual Basic for Applications para a determinação da descarga sólida total a partir dos dados obtidos na Pequena Central Hidrelétrica de Mogi-Guaçu (SP-Brazil). Foi verificada a redução da descarga sólida total no reservatório entre as campanhas, resultados esses condizentes com o esperado. Além disso, comparando-se os resultados fornecidos pela ferramenta computacional desenvolvida com outros softwares, as diferenças foram mínimas e comprovam a validade e consistência do método implementado. Ressalta-se também que a metodologia utilizada no estudo de caso pode ser replicada para outros locais, proporcionando mais informações para a gestão e planejamento de recursos hídricos.

Palavras-chave: Hidrossedimentologia; Descarga sólida total; Ferramenta computacional; Visual basic for Applications

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1 Introduction

Brazil has one of the biggest hydro energetic reserves in the world, along with a vast amount of world's fresh water. This resource is mainly used for irrigation, storage and electric power generation, which require hydro-sedimentological analysis the knowledge of the water body, indispensable to its water resource management and correct use. Moreover, the hydro-sedimentological processes demand sediment detailed studies and its interactions with the environment, an important theme of economical, social and ecological interest.

Syvistki et al. (2005) claim that environmental issues related to sediments are particularly important in developing countries, since its population growth rate is usually high and this increase is proportional to the pressure over natural resources, which causes the rates of production and deposition of sediment to rise. Once it is present in the aquatic ecosystem, it plays an important role to the biota supplying nutrients and energy. Besides, sediment performs as a water quality regulator due to its capacity to withhold and release pollutants (GOLTERMAN; SLY; THOMAS, 1983). According to Carvalho (2008) and Vanoni (1975), the sediment transport may: jeopardize all the water uses; interfere with the light penetration and the heat in the water bodies; needed to the photosynthesis and salubrity in the water bodies; act as carriers for other pollutants; cause abrasion in electromechanical equipment and hydraulic structures; and provoke disturbances in the channel shape.

Generically, according to Branco e Rocha (1977) e Muller (1995), all watercourses have the intrinsic property to transport sediments, whether suspended, saltation, rolling or a combination of these ways. The sediment transport in water is ruled by the relation between the water discharge carrying capacity and the strength needed to shift the solid particles available in its course (LIMA; SILVA, 2007).

Curtis, Culbertson e Chase (1973) used data from 27 drainage basins in USA could estimate the yearly average sediment discharge that reached the oceans. The results pointed that 14.2 million of tons per day of sediment reached the Atlantic Ocean, 378.179 million reached the Gulf of Mexico, and 99.1 million reached the Pacific Ocean. Furthermore, to Curtis, Culbertson e Chase (1973) and Holeman (1968), it is estimated that in USA only about 10% of eroded material in the drainage basins reach oceans, while the rest is deposited in lakes, reservoirs, channels and land surface. Syvitski et al. (2005) verified that 12.6 billion of tons of sediment per year are carried worldwide in water bodies, considering that reservoirs trap 20% of global sediment inflow due mostly to the deposition and yield.

According to Silva e Wilson Júnior (2005), the sediment discharge estimate in a river is probably one of the most complex problems in all fluvial hydraulics. The suspended load is always easily attained. The biggest difficulty, according to Carvalho (2008) e Paiva (2001), is in the assessment of bed and total load as a result of more quantities involved. They can be classified as de-

terministic processes, which use equations to estimate these processes, or in stochastic processes (probability) that use data acquired in field work to analyze the correlation between the involved variables.

Among the most known estimate methods of total sediment discharge worldwide are the Modified Einstein Procedure by Colby and Hembre (1955) and the Simplified Procedure by Colby (1957). The former procedure is a probabilistic method, result of several years of research of shallow and deep rivers in Nebraska, USA. In this case, suspended load measures and bed load gathering are needed, which requires lots of information and the use of abacuses (Santos, et al., 2012). The latter procedure by Colby (1957) to estimate total sediment discharge is based on Einstein's procedure and in several field measurements. In this assessment, the total sediment discharge is separated in measured and unmeasured; the first is easily calculated using total sediment discharge equations, meanwhile the second is estimated using abacuses.

However, to Alonso, Neibling e Foster (1981), the forethought of sediment transport rates significantly differs between the formulas, which turns the choosing of a reliable equation to estimate a specific load difficult. Scapin, Paiva e Beling (2007) found that the Procedures, both the Modified Einstein and Colby, that incorporate suspended sediment concentration measured data, provided the best results in a section from the river Arroio Cancela in Santa Maria (RS).

Considering the total sediment discharge estimation procedures' potential to support hydro-sedimentological studies, a case study was made using a hydro-sedimentological module from a computational tool developed by one of its authors, written in Visual Basic for Applications (VBA) to determine the total sediment discharge using data acquired from the Mogi-Guaçu Small Hydro Electric Power Plant (SP-Brazil).

This study is part of a project from the Technological Research and Development Program from Electrical Energy Sector (P&D ANEEL) through a partnership between São Carlos School of Engineering, Foundation for the Research Increase and the Industrial Improvement (FIPAI) and the Energy Company AES Tietê, the latter being the project's sponsor.

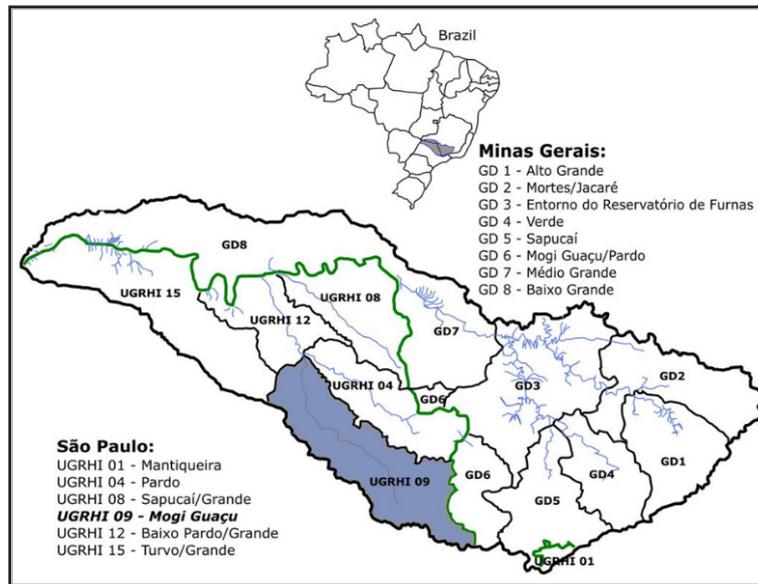
2 Materials and Methods

2.1 Study area characterization

The study area to gather the required data to the computational tool tests was the reservoir from the Mogi-Guaçu Small Hydro Electric Power Plant. It is located in Mogi-Guaçu drainage basin (22°22'45.6" S; 46°53'59,1" W), and belongs to Water Resources Management Unity 9 (UGRHI - 9) (Figure 1).

The Mogi-Guaçu Small Hydro Electric Power Plant (SP-Brazil) is located in the Alto Mogi sub-drainage basin, between the cities Mogi-Guaçu and Mogi-Mirim. The river Mogi-Guaçu gives its name to both to the city and the undertaking, that has a head of 11.6m and 7.2 MW of installed capacity power (Figure 2). It

Figure 1 – State of São Paulo Water Resources Management Unities



Source: Santos et al. (2018)

Figure 2 – Mogi-Guaçu Small Hydro Electric Power Plant aerial view



Source: AES Tietê (2018)

was originally owned by Companhia Energética de São Paulo (CESP) but was later acquired by AES Tietê in late 90's during the great privatization of the electric power industry and remains under the concession of this company (Table 1).

According to CBH Mogi (2008), the waters from the

Mogi-Guaçu Small Hydropower Plant's reservoir are ranked as Class 2, its surroundings is mostly used to plant sugar cane with small pasture areas and coffee plant cultivation. Its influence area is in a zone identified as of high susceptibility to erosion, as well as a large portion of the reservoir's drainage basin area.

Table 1 – Mogi-Guaçu (SP) Small Hydropower Plant Characteristics

Mogi-Guaçu (SP) Small Hydropower Plant Technical Characteristics			
Operation start	1994	Installed capacity power	7.2 MW
Location	Mogi-Guaçu river	Turbines	2
Flooded area	5.73 km ²	Nominal voltage	13.8 kV
Volume	32.89 x 10 ⁶ m ³	Maximum operating water level	598.5 m
Dam length	150 m	Minimum operating water level	596 m
Total water discharge in the spillway	2,099 m ³ .s ⁻¹	Sluice gate	No

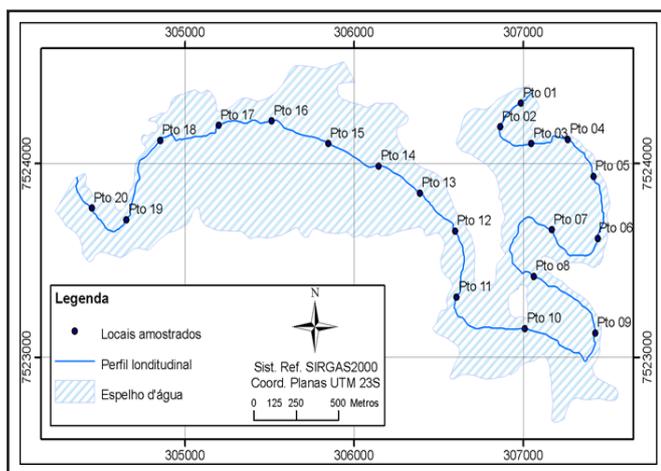
Other than the electric power generation, the dam also damps the peak flood of rain episodes and provide for the cities Mogi-Mirim and Mogi-Guaçu. Both towns have high susceptibility areas in their urban area to floods throughout the Mogi-Guaçu river banks downstream of the dam.

2.2 Primary data gathering

Primary data gathering in the Mogi-Guaçu reservoir took place in two surveys. The first one, representing the rainy season, happened on January 25, 27, 28 and 29, 2014. The second one, representing the drought season, happened on March 18, 19 and 20, 2014.

For that, the reservoir was strategically divided into 20 sampling locations for a better understanding of the sediment transport throughout it, whereas each location was located approximately over the talweg (Figure 3). Moreover, measurements were made throughout the cross section on locations 12, 14, 16 and 20, located in the reservoir's main channel. It is worth noting that on the second survey, there were algae preventing the access to location 20, therefore the measurements were up to location 19.

Figure 3 – Mogi-Guaçu reservoir sampling locations



Source: FIPAI (2015)

The precise location of the sampling locations was obtained using a high precision GPS receptor, model GS20, with an antenna, model AT 201 from Leica Geosystems, that was installed along a 1,200 kHz ADCP. The ADCP was coupled besides the ship pointing downwards, approximately 40 cm deep (Figure 4). ADCPs uses the Doppler Effect, assess the water discharge mean direction, projecting the velocity onto a normal plane in this direction. This projection allows the calculation of the water discharge. In short, the ADCP supplied hydraulic data for width, depth, total section area, velocity, water discharge, among other information. The measurements were done two to four times in the same section to obtain a mean value, reminding that the ADCP can't measure all the cross section.

Figure 4 – ADCP assembly design with GPS antenna inside the boat (Above); ADP not yet submerged (Bellow)



Source: Authors

Samples of the suspended sediment concentration (SSC) were collected using the Van Dorn Bottle to sample water-sediment at the surface, approximately 1 meter deep, and close to the bottom, at least 0.5 m distant from the riverbed). All procedures to determine the concentration of suspended solids were carried out following the norms and procedures proposed in the Standard Methods for Examination of Water and Wastewater (APHA, 1995).

2.3 Total sediment discharge calculation's implementation

The computational tool (NH Statistic and Sediment) was written in Visual Basic for Applications (VBA) programming language. This type of language was chosen due to the abundance and flexibility of its features, and mainly due to the great availability and ease of access, user-friendly and intuitive interface, including interactivity with Access® databases.

Among the methods to determine and assess the total sediment discharge, Colby's simplified procedure (COLBY, 1957) was chosen. According to Miranda (2015), this method compared to the Einstein procedure modified by Colby and Hembree (1955) requires less data, which

makes it more economical and easier, precisely by the reduction of field and laboratory work.

Colby (1957) showed correlations between unmeasured sediment discharge with mean velocity and concentration and verified the possibility of these correlations being successfully applied to several types of sediment assessments. Thus, the total sediment discharge is given by Equation 1.

$$Q_{st} = Q_{sm} + Q_{nm} \quad (1)$$

Where:

Q_{st} = total sediment discharge [t.day⁻¹];

Q_{ss} = measured sediment [t.day⁻¹];

Q_{nm} = unmeasured sediment [t.day⁻¹];

The measured sediment (Q_{sm}) can be obtained by calculating the suspended load (Equation 2). However, the unmeasured sediment (Q_{nm}), given by Equation 3, which represents the integration of bed load with unmeasured load, is estimated with the aid of abacuses, knowing the mean velocity (ms⁻¹), depth (m), measured concentration (ppm) and section width (m) (CARVALHO, 2008).

$$Q_{sm} = 0.0864 \cdot Q \cdot CSS \quad (2)$$

$$Q_{nm} = q'_{nm} \cdot k \cdot L \quad (3)$$

Where:

Q = water discharge [m³.s⁻¹];

CSS = measured or sampled concentration [ppm = mg.L⁻¹];

q'_{nm} = unmeasured sediment per one meter of the water body's cross section width [t.day⁻¹.m⁻¹];

L = sampled cross section width [m];

k = correction factor [dimensionless];

Figure 5 contains the Abacus 1 of the simplified procedure by Colby (1957). In it, it is possible to obtain the unmeasured sediment per meter of width of the water body from the mean water discharge velocity. The software Engauge Digitizer developed by Mitchell et al. (2018) was used to obtain a representative equation for Abacus 1, which automatically retrieves data points from graphs, thus allowing an equation to be coded in VBA (Equation 4).

$$\log \log q'_{nm} = 3.340 \cdot \log \log V + 1.617 \quad (4)$$

After that, it was still necessary to determine the correction factor k , obtained from Abacus 2 and 3. Figure 5 presents Abacus 2 that allows the relative concentration (C_r) to be obtained using velocity and mean depth. In this case, the equations used for Abacus 2 coding were listed by Paiva (1988).

According to the author, the relative concentration is given by Equation 5.

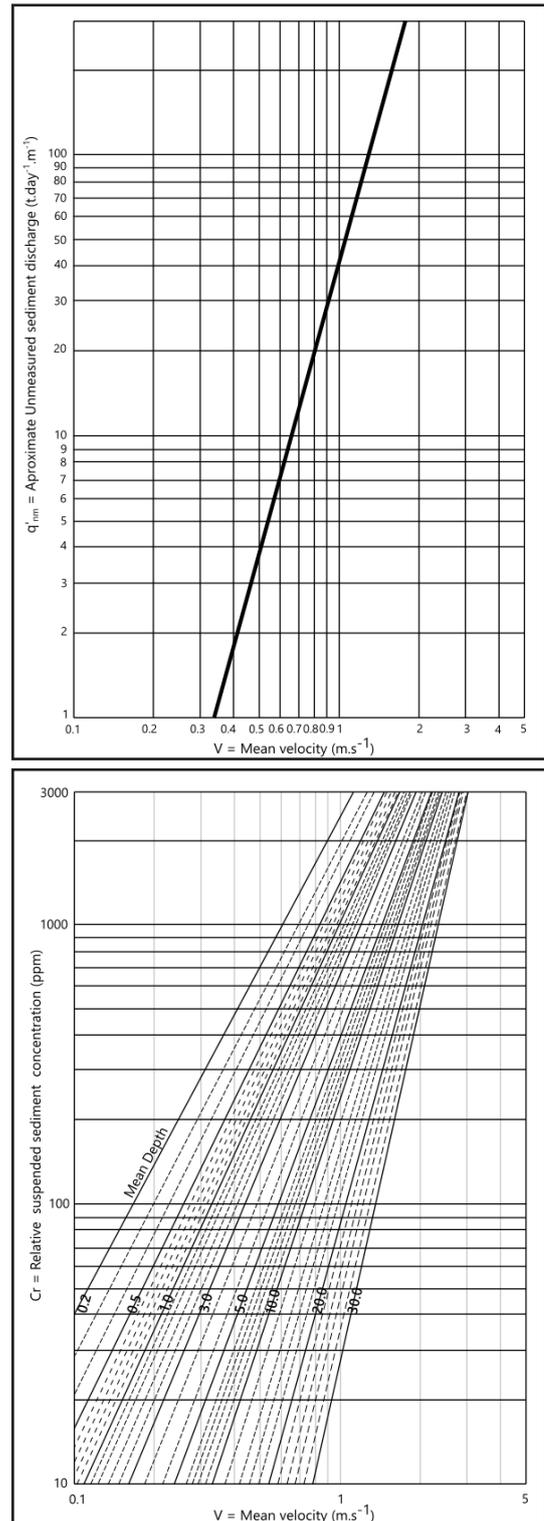
$$\log \log C_r = A \cdot \log \log V + B \quad (5)$$

Where:

C_r = Relative concentration [ppm = mg.L⁻¹];

A e B = Standard values to obtain C_r data by Paiva (1988, p.275)

Figure 5 – Abacus 1: Acquiring of unmeasured sediment discharge per one meter of the water body's cross section width using mean velocity (Above); Abacus 2: Acquiring of relative sediment concentration using mean velocity and mean depth (Bellow)

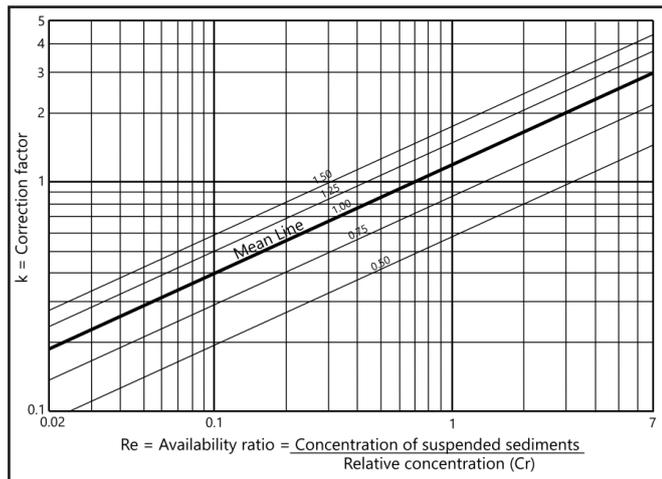


Source: Adapted from Carvalho (2008) and Paiva (2001)

After determining the relative concentration (C_r), from Equation 6 it was possible to determine the efficiency ratio (Re) given by the ratio of the measured concentration to the relative concentration. Thus, through Abacus 3, we could determine the correction factor k (Figure 6).

$$Re = \frac{SSC}{C_r} \quad (6)$$

Figure 6 – Abacus 3: Acquiring correction factor using availability ratio



Source: Adapted from Carvalho (2008) and Paiva (2001)

As in previous abacuses, according to Colby (1957), abacus 3 represents the wide range of cross sections and concentrations measured in several rivers such as Mississippi, Colorado and Niobrara in the United States. Therefore, the mean line represents the location of most of the 262 points plotted in the author's study, which makes it the best curve for this application. In this case, the Engauge Digitizer software was used to determine the mean line equation in Abacus 3 (Equation 7).

$$\log \log k = 0.4819 \cdot \log \log Re + 0.0739 \quad (7)$$

Knowing all the procedure that involves the estimation of total sediment discharge as well as the equations that rule it, the Colby procedure (1957) in the computational tool was implemented in VBA code, allowing the Q_{st} to be estimated for different sections of the Mogi-Guaçu reservoir.

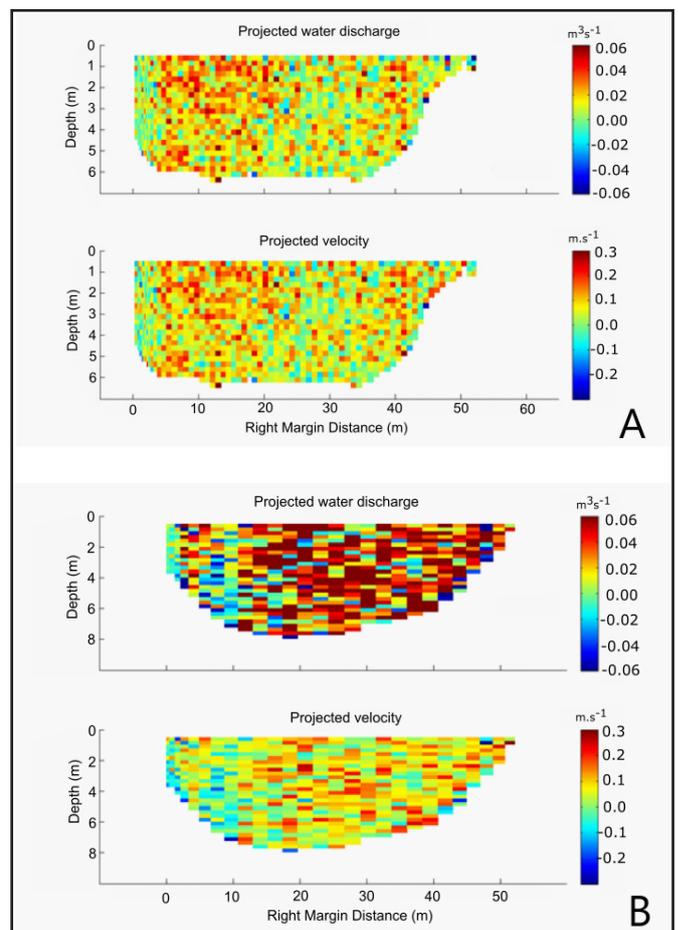
3 Results and Discussion

Figures 7 and 8 illustrate some of the water discharge and velocity profiles obtained in the measurements of the hydraulic characteristics of the Mogi-Guaçu reservoir sections, respectively at the entrance of the reservoir and near the dam.

Analyzing the velocity profiles, it is clear that the water discharge intensity in the broader sections in both campaigns decreased. The cell velocities in section 1 were observed mostly between 0.0 and 0.3 $m \cdot s^{-1}$, while in sections

19 and 20 cell velocities were between -0.1 and 0.1 $m \cdot s^{-1}$. It is worth noting that negative velocity values indicate that the water discharge is in the opposite direction, which is present in flooded areas resulting from natural turbulence of the water bodies. The results of the hydraulic and sedimentological characteristics are presented in Tables 2 and 3, respectively, for the first and second surveys. Table 3 - Hydraulic characteristics' measurements of Mogi-Guaçu's reservoir in the second survey

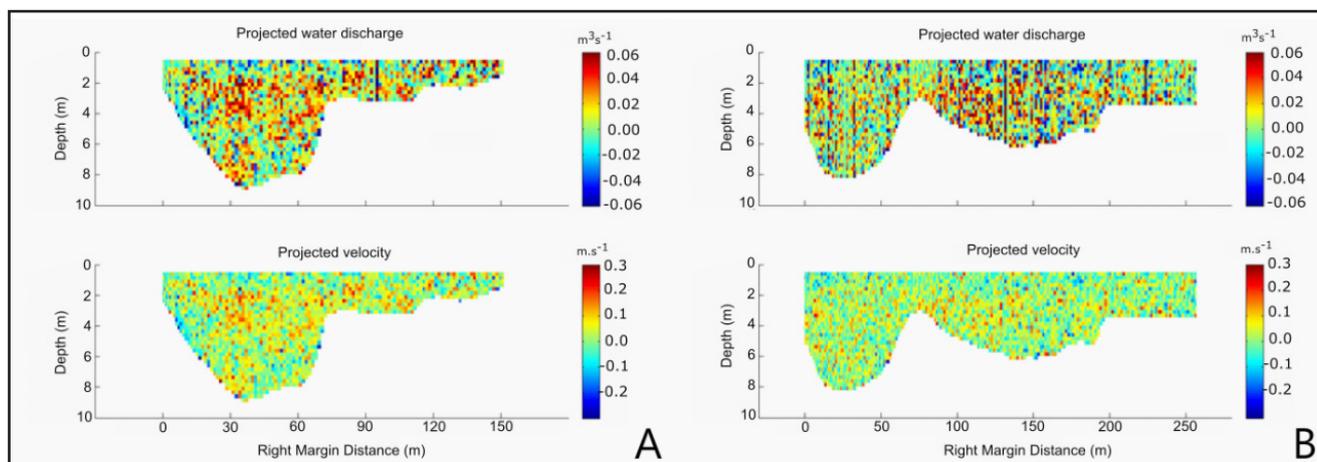
Figure 7: (a) Estimated water discharge and velocity: Section 1 second measurement in the first survey; and (b) Section 1 first measurement in the second survey



Source: FIPAI

With the exception of the results of section 16, it was noticed that the water discharge in all the sections presented similar results, ranging from 20.76 to 28.67 $m^3 \cdot s^{-1}$. Regarding section 16, because of its greater width in the reservoir along with the intensity of the winds, that varies between 0.219 and 0.533 $m \cdot s^{-1}$ in the first campaign and 0.780 and 1.256 $m \cdot s^{-1}$ in the second one, there were difficulties in measuring because of the waves formed in the reservoir that prevented the ADCP from being vertical 100% of the time, impairing the quality of results for this section in both campaigns.

Figure 8: (a) Estimated water discharge and velocity: Section 20 third measurement in the first survey; and (b) Section 19 first measurement in the second survey



Source: FIPAI

Table 2 - Hydraulic and sedimentological characteristics' measurements of Mogi-Guaçu's reservoir cross sections in the second survey

Section	Measurement	Mean water discharge ($\text{m}^3 \cdot \text{s}^{-1}$)	Mean Velocity ($\text{m} \cdot \text{s}^{-1}$)	Width (m)	Mean Depth (m)	SSC ($\text{mg} \cdot \text{L}^{-1}$)
Section 1	S1-1	24.22	0.064	61.29	6.45	59.000
	S1-2	21.83	0.06	58.57	6.34	
	S1-3	21.65	0.058	60.1	6.32	
	S1-4	22.31	0.064	57.74	6.20	
Section 6	S6-1	22.64	0.086	48.02	5.91	52.500
	S6-2	22.95	0.081	49.4	6.21	
	S6-3	24.93	0.086	50.41	6.10	
	S6-4	22.5	0.076	51.27	6.25	
Section 8	S8-1	21.77	0.066	58.53	6.72	45.000
	S8-2	22.03	0.057	57.04	6.69	
	S8-3	22.89	0.062	56.81	6.71	
	S8-4	22.83	0.059	58.91	6.67	
Section 12	S12-1	27.61	0.045	117.56	6.22	35.500
	S12-2	22.76	0.04	120.81	6.13	
	S12-3	24.8	0.042	118.59	6.18	
	S12-4	20.76	0.038	128.8	5.93	
Section 16	S16-4	21.77	0.013	667.56	4.40	25.000
	S20-1	27.39	0.033	160.11	5.36	
Section 20	S20-2	24.87	0.038	158.68	5.40	19.670
	S20-3	22.06	0.026	152.33	5.59	
	S20-4	22.62	0.037	154.81	5.69	

Source: FIPAI (2015)

Table 3 – Hydraulic characteristics' measurements of Mogi-Guaçu's reservoir in the second survey

Section	Measurement	Mean water discharge (m ³ .s ⁻¹)	Mean Velocity (m.s ⁻¹)	Width (m)	Mean Depth (m)	SSC (mg.L ⁻¹)
Section 1	S1-1	21.09	0.051	51.31	7.54	20.000
	S1-2	16.8	0.05	54.8	7.46	
	S1-3	20.45	0.051	56.83	7.36	
Section 6	S6-1	20.01	0.051	52.13	6.69	15.500
	S6-2	19.38	0.056	55.44	6.45	
	S6-3	19.37	0.054	54.36	6.62	
Section 8	S8-1	20.78	0.053	58.54	6.88	14.000
	S8-2	20.72	0.053	56.93	7.23	
	S8-3	24.36	0.06	57.77	7.11	
Section 12	S12-1	28.53	0.042	113.27	6.79	20.500
	S12-2	26.5	0.038	118.21	6.50	
	S12-3	28.67	0.04	112.93	6.75	
Section 16	S16-1	40.38	0.022	616.41	3.15	14.862
	S16-2	35.21	0.024	625.81	2.99	
	S16-3	41.26	0.021	622.87	3.27	
Section 19	S19-1	24.51	0.025	258.3	6.13	8.942
	S19-2	23.47	0.015	264.95	5.93	
	S19-3	18.08	0.018	264.92	5.96	

Source: FIPAI (2015)

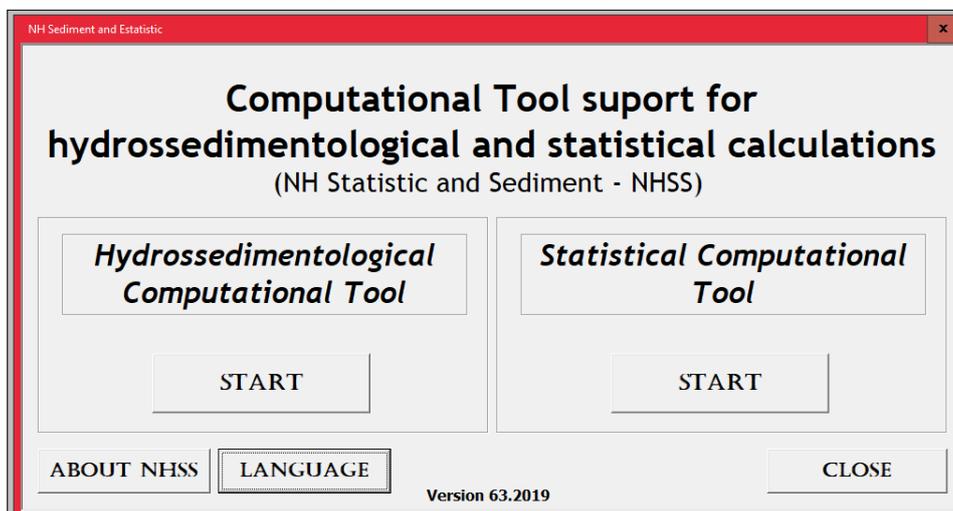
3.1 Simulations in the developed computational tool

The NH Statistic and Sediment Computational Tool (NHSS) has a hydro-sedimentological module and a statistic one that can be selected by the user according to their objectives (Figure 9). In this paper, we present the hydro-sedimentological module that uses Colby's procedure (1957) to estimate the total solid discharge

in water bodies (Figure 10). The tool allows the user to enter the data of water discharge (m³.s⁻¹), mean velocity (ms⁻¹), width (m), mean depth (m) and mean concentration (mg.L⁻¹) in the fields highlighted in yellow and the results obtained are shown in the gray fields.

Figure 11 shows the screen with the data used in the computational tool to estimate the total sediment discharge for the first survey and Table 4 presents a summary containing the respective obtained results. The values

Figure 9 – Total sediment discharge estimate screen using Colby's simplified procedure (1957)



Source: Santos (2019)

Figure 10 – Total sediment discharge estimate screen using Colby’s simplified procedure (1957)



Source: Santos (2019)

of sediment discharge presented mean values in the sections of the Mogi-Guaçu reservoir varying between 117.68 t.day⁻¹ (Section 1) and 42.33 t.day⁻¹ (Section 20). In addition, the Qst decrease along the reservoir was observed mainly in sections 12, 16 and 20 due to the increase in the width of the reservoir where there is a reduction in the depth which identifies the formation of a sediment deposition delta. In these sections, the classes of greater granulometry were deposited, reducing the amount of sediment being transported.

In order to compare and verify the temporal variation of the Qst in the Mogi-Guaçu reservoir, Figure 12 shows the screen with the data used in the computational tool to estimate the total sediment discharge for the second survey and Table 5 contains the obtained results.

In this case, it was possible to observe that mean values of total sediment discharge varied between 17.45

t.day⁻¹ (Section 19) and 50.97 t.day⁻¹ (Section 12). The values of Qst presented in Table 5 are significantly lower than the data obtained in survey 1, precisely because of water discharge and lower suspended sediment concentrations. Besides, this characteristic was expected due to survey 2 being associated to the dry season of the hydrological year.

It should be noted that the high Qst obtained mainly in section 16 are related to the biggest measured water discharges. It is believed that this increase in water discharge is related to the difficulties in the measurements of the hydraulic characteristics of the section with the ADCP, since the wind speed made it difficult to obtain data. Despite this, the estimates of total sediment discharge by the simplified procedure by Colby (1957) obtained with the NH Statistic and Sediment Computational Tool are consistent between the two surveys.

Figure 11 – Total sediment discharge calculation in different sections (Survey 1)

n	Measurement	Water Discharge (m³/s)	Mean Velocity (m/s)	Width (m)	Depth (m)	Suspended Sediment Concentration (mg/L)	Measured Solid Discharge - Qss (t/day)	Unmeasured Solid Discharge - Qnm (t/day)	Total Solid Discharge - Qst (t/day)
1	S1-1	24.220	0.064	61.290	6.450	59.000	123.4639	3.338	126.801
2	S1-2	21.830	0.060	58.570	6.339	59.000	111.2806	2.768	114.049
3	S1-3	21.650	0.058	60.100	6.316	59.000	110.3630	2.637	113.000
4	S1-4	22.310	0.064	57.740	6.198	59.000	113.7275	3.144	116.872
5	S6-1	22.640	0.086	48.020	5.907	52.500	102.6950	4.726	107.421
6	S6-2	22.950	0.081	49.400	6.210	52.500	104.1012	4.263	108.364
7	S6-3	24.930	0.086	50.410	6.102	52.500	113.0825	4.961	118.043
8	S6-4	22.500	0.076	51.270	6.247	52.500	102.0600	3.847	105.907
9	S8-1	21.770	0.066	58.530	6.725	45.000	84.6418	3.574	88.215
10	S8-2	22.030	0.057	57.040	6.686	45.000	85.6526	2.545	88.198
11	S8-3	22.890	0.062	56.810	6.711	45.000	88.9963	3.034	92.031
12	S8-4	22.830	0.059	58.910	6.666	45.000	88.7630	2.830	91.593
13	S12-1	27.610	0.045	117.560	6.223	35.500	84.6854	2.315	87.000
14	S12-2	22.760	0.040	120.810	6.132	35.500	69.8095	1.837	71.647
15	S12-3	24.800	0.042	118.590	6.178	35.500	76.0666	2.007	78.074
16	S12-4	20.760	0.038	128.800	5.926	35.500	63.6751	1.750	65.425
17	S16-4	21.770	0.013	667.560	4.402	25.000	47.0232	0.491	47.514
18	S20-1	27.390	0.033	160.110	5.356	19.670	46.5490	1.026	47.575
19	S20-2	24.870	0.038	158.680	5.395	19.670	42.2663	1.392	43.658
20	S20-3	22.060	0.026	152.330	5.594	19.670	37.4907	0.678	38.168
21	S20-4	22.620	0.037	154.810	5.685	19.670	38.4424	1.493	39.935

Source: Authors

Table 4 - Total sediment discharge data synthesis obtained in the Computational tool NHSS (Survey 1)

Sections	Measurement	Mean water discharge (m ³ .s ⁻¹)	SS _c (mg.L ⁻¹)	Measured load - Q _{ss} (t.dia ⁻¹)	Unmeasured load - Q _{nm} (t.dia ⁻¹)	Total solid discharge - Q _{st} (t.dia ⁻¹)
Section 1 (S1)	S1-1	24.22	59.000	123.464	3.338	126.801
	S1-2	21.83		111.281	2.768	114.049
	S1-3	21.65		110.363	2.637	113.000
	S1-4	22.31		113.727	3.144	116.872
Section 6 (S6)	S6-1	22.64	52.500	102.695	4.726	107.421
	S6-2	22.95		104.101	4.263	108.364
	S6-3	24.93		113.082	4.961	118.043
	S6-4	22.5		102.060	3.847	105.907
Section 8 (S8)	S8-1	21.77	45.000	84.642	3.574	88.215
	S8-2	22.03		85.653	2.545	88.198
	S8-3	22.89		88.996	3.034	92.031
	S8-4	22.83		88.763	2.830	91.593
Section 12 (S12)	S12-1	27.61	35.500	84.685	2.315	87.000
	S12-2	22.76		69.809	1.837	71.647
	S12-3	24.8		76.067	2.007	78.074
	S12-4	20.76		63.675	1.750	65.425
Section 16 (S16)	S16-4	21.77	25.000	47.023	0.491	47.514
Section 20 (S20)	S20-1	27.39	19.670	46.549	1.026	47.575
	S20-2	24.87		42.266	1.392	43.658
	S20-3	22.06		37.491	0.678	38.168
	S20-4	22.62		38.442	1.493	39.935

Figure 12 - Total sediment discharge calculation in different sections (Survey 2)

n	Measurement	Water Discharge (m ³ /s)	Mean Velocity (m/s)	Width (m)	Depth (m)	Suspended Sediment Concentration (mg/L)	Measured Solid Discharge - Q _{ss} (t/day)	Unmeasured Solid Discharge - Q _{nm} (t/day)	Total Solid Discharge - Q _{st} (t/day)
1	S1-1	21.090	0.051	51.310	7.544	20.000	36.4435	1.281	37.725
2	S1-2	16.800	0.050	54.800	7.463	20.000	29.0304	1.250	30.280
3	S1-3	20.450	0.051	56.830	7.363	20.000	35.3376	1.352	36.690
4	S6-1	20.010	0.051	52.130	6.688	15.500	26.7974	1.097	27.895
5	S6-2	19.380	0.056	55.440	6.454	15.500	25.9537	1.183	27.136
6	S6-3	19.370	0.054	54.360	6.625	15.500	25.9403	1.293	27.233
7	S8-1	20.780	0.053	58.540	6.884	14.000	25.1355	1.274	26.409
8	S8-2	20.720	0.053	56.930	7.230	14.000	25.0629	1.239	26.302
9	S8-3	24.360	0.060	57.770	7.107	14.000	29.4659	1.639	31.105
10	S12-1	28.530	0.042	113.270	6.792	20.500	50.5323	1.801	52.333
11	S12-2	26.500	0.038	118.210	6.500	20.500	46.9368	1.233	48.170
12	S12-3	28.670	0.040	112.930	6.745	20.500	50.7803	1.618	52.398
13	S16-1	40.380	0.022	616.410	3.151	14.862	51.8510	0.705	52.556
14	S16-2	35.210	0.024	625.810	2.993	14.862	45.2123	0.878	46.091
15	S16-3	41.260	0.021	622.870	3.272	14.862	52.9810	0.638	53.619
16	S19-1	24.510	0.025	258.300	6.135	8.942	18.9362	0.721	19.657
17	S19-2	23.470	0.015	264.950	5.932	8.942	18.1327	0.241	18.374
18	S19-3	18.080	0.018	264.920	5.955	8.942	13.9684	0.360	14.328

Source: Authors

Table 5 – Total sediment discharge data synthesis obtained in the Computational tool NHSS (Survey 2)

Sections	Measurement	Mean water discharge (m ³ .s ⁻¹)	SS ₂₀ (mg.L ⁻¹)	Measured load – Q _{ss} (t.dia ⁻¹)	Unmeasured load – Q _{nm} (t.dia ⁻¹)	Total solid discharge – Q _{st} (t.dia ⁻¹)
Section 1 (S1)	S1-1	21.09		36.444	1.281	37.725
	S1-2	16.8	20.000	29.030	1.250	30.280
	S1-3	20.45		35.338	1.352	36.690
Section 6 (S6)	S6-1	20.01		26.797	1.097	27.895
	S6-2	19.38	15.500	25.954	1.183	27.136
	S6-3	19.37		25.940	1.293	27.233
Section 8 (S8)	S8-1	20.78		25.135	1.274	26.409
	S8-2	20.72	14.000	25.063	1.239	26.302
	S8-3	24.36		29.466	1.639	31.105
Section 12 (S12)	S12-1	28.53		50.532	1.801	52.333
	S12-2	26.5	20.500	46.937	1.233	48.170
	S12-3	28.67		50.780	1.618	52.398
Section 16 (S16)	S16-1	40.38		51.851	0.705	52.556
	S16-2	35.21	14.862	45.212	0.878	46.091
	S16-3	41.26		52.981	0.638	53.619
Section 19 (S19)	S19-1	24.51		18.936	0.721	19.657
	S19-2	23.47	8,42	18.133	0.241	18.374
	S19-3	18.08		13.968	0.360	14.328

3.2 Verification of the total sediment discharge results obtained in the computational tool - NH Statistic and Sediment

For the comparison of the total sediment discharge results obtained by the NH Statistic and Sediment computational tool, they were compared with two other computational tools: WinTSR (ROSA; BERLING, 2002) and NH Sediment (MIRANDA, 2015). The results obtained from the simulations in these two software (WinTSR and NH Sediment) as well as the comparison with the NH Statistic and Sediment (NHSS) data are presented in Tables 6 to 9. Comparing the Q_{st} values obtained by the developed computational tool and the WinTSR it was possible to observe a low percentage difference between the applications, with an average of -0.30%. In relation to NH Sediment, the average percentage difference was 0.73% for the first survey. Despite the greater difference between the tools NH Statistic and Sediment and NH Sediment, in both cases this difference is minimal and does not mitigate future sediment transport studies in the region and shows the accuracy of the developed tool.

Analyzing the data from survey 2, it was observed that, as in survey 1, the Q_{st} differences between the software were minimal, with mean values of -0.30% and 0.89%, respectively, in relation to WinTSR and NH Sediment.

Table 10 presents the comparisons of the sediment discharge involving the two surveys in ascending order regarding the Q_{st} obtained in the developed computatio-

nal tool. In addition, WinTSR was adopted as standard comparison software due to its wide use in studies such as Scapin, Paiva and Beling (2007), Santos et al. (2012), Miranda (2015).

Q_{st} values were ordered in relation to the WinTSR software but no percentage difference pattern was found. In other words, there are major and minor errors evenly distributed among the results. This indicates that the total sediment discharge results provided by the computational tool are consistent and valid.

Thus, it was possible to observe that the computational tool NH Statistic and Sediment presented values of total sediment discharge compatible with the other software. Comparisons with WinTSR showed that the developed tool NHSS provided better results than the NH Sediment tool, since the maximum percentage difference between WinTSR and NHSS was -0.49% while between WinTSR and NH Sediment was -1.66%. Despite this, the results among all the software are satisfactory and meet the objective of estimating the total sediment discharge with maximum reliability.

Overall, the computational tool NH Statistic and Sediment allows the calculation of the Q_{st} of several sections/locations in a single click, while in WinTSR this parameter is obtained from section to section. In addition, unlike WinTSR and NH Sediment, which are software aimed at hydro-sedimentology, the NH Statistic and Sediment computational tool is a multidisciplinary software that also performs statistical calculations, at no cost, open

Table 6 – Comparison between the total sediment discharge values (Qst) obtained in the NHSS computational tool and WinTSR software (Survey 1)

Section	Qst - NHSS (t.day ⁻¹)	Qst - WinTSR (t.day ⁻¹)	Difference between Qst (WinTSR and NHSS) (t.day ⁻¹)	Difference between Qst (WinTSR and NHSS) (%)
S1-1	126.801	126.467	-0.335	-0.26%
S1-2	114.049	113.768	-0.281	-0.25%
S1-3	113.000	112.731	-0.270	-0.24%
S1-4	116.872	116.556	-0.315	-0.27%
S6-1	107.421	106.979	-0.442	-0.41%
S6-2	108.364	107.961	-0.404	-0.37%
S6-3	118.043	117.580	-0.464	-0.39%
S6-4	105.907	105.538	-0.369	-0.35%
S8-1	88.215	87.856	-0.359	-0.41%
S8-2	88.198	87.934	-0.264	-0.30%
S8-3	92.031	91.722	-0.309	-0.34%
S8-4	91.593	91.216	-0.377	-0.41%
S12-1	87.000	86.761	-0.239	-0.28%
S12-2	71.647	71.453	-0.194	-0.27%
S12-3	78.074	77.864	-0.210	-0.27%
S12-4	65.425	65.239	-0.187	-0.29%
S16-4	47.514	47.456	-0.058	-0.12%
S20-1	47.575	47.470	-0.105	-0.22%
S20-2	43.658	43.520	-0.138	-0.32%
S20-3	38.168	38.094	-0.074	-0.19%
S20-4	39.935	39.782	-0.153	-0.38%

Table 7 – Comparison between the total sediment discharge values (Qst) obtained in the NHSS computational tool and NH Sediment computation tool (Survey 1)

Section	Qst - NHSS (t.day ⁻¹)	Qst - NH Sediment (t.day ⁻¹)	Difference between Qst (NH Sediment e NHSS) (t.day ⁻¹)	Difference between Qst (NH Sediment e NHSS) (%)
S1-1	126.801	127.580	0.779	0.61%
S1-2	114.049	114.721	0.672	0.59%
S1-3	113.000	113.654	0.654	0.58%
S1-4	116.872	117.605	0.734	0.62%
S6-1	107.421	108.309	0.888	0.82%
S6-2	108.364	109.202	0.838	0.77%
S6-3	118.043	118.976	0.933	0.78%
S6-4	105.907	106.699	0.791	0.74%
S8-1	88.215	89.041	0.825	0.93%
S8-2	88.198	88.842	0.644	0.73%
S8-3	92.031	92.760	0.729	0.79%
S8-4	91.593	92.294	0.701	0.76%
S12-1	87.000	87.636	0.636	0.73%
S12-2	71.647	72.184	0.538	0.74%
S12-3	78.074	78.646	0.572	0.73%
S12-4	65.425	65.951	0.526	0.80%
S16-4	47.514	47.734	0.220	0.46%
S20-1	47.575	47.884	0.309	0.65%
S20-2	43.658	44.047	0.389	0.88%
S20-3	38.168	38.403	0.235	0.61%
S20-4	39.935	40.369	0.434	1.08%

Table 8 – Comparison between the total sediment discharge values (Qst) obtained in the NHSS computational tool and WinTSR software (Survey 2)

Section	Qst - NHSS (t.day ⁻¹)	Qst - WinTSR (t.day ⁻¹)	Difference between Qst (WinTSR and NHSS) (t.day ⁻¹)	Difference between Qst (WinTSR and NHSS) (%)
S1-1	37.725	37.596	-0.129	-0.34%
S1-2	30.280	30.156	-0.125	-0.41%
S1-3	36.690	36.555	-0.135	-0.37%
S6-1	27.895	27.787	-0.107	-0.39%
S6-2	27.136	27.027	-0.109	-0.40%
S6-3	27.233	27.109	-0.124	-0.46%
S8-1	26.409	26.287	-0.122	-0.46%
S8-2	26.302	26.183	-0.119	-0.45%
S8-3	31.105	30.952	-0.153	-0.49%
S12-1	52.333	52.146	-0.187	-0.36%
S12-2	48.170	48.044	-0.126	-0.26%
S12-3	52.398	52.229	-0.169	-0.32%
S16-1	52.556	52.593	0.037	0.07%
S16-2	46.091	46.138	0.047	0.10%
S16-3	53.619	53.653	0.034	0.06%
S19-1	19.657	19.578	-0.079	-0.41%
S19-2	18.374	18.342	-0.032	-0.17%
S19-3	14.328	14.285	-0.043	-0.30%

Table 9 – Comparison between the total sediment discharge values (Qst) obtained in the NHSS computational tool and NH Sediment computation tool (Survey 2)

Section	Qst - NHSS (t.day ⁻¹)	Qst - NH Sediment (t.day ⁻¹)	Difference between Qst (NH Sediment and NHSS) (t.day ⁻¹)	Difference between Qst (NH Sediment and NHSS) (%)
S1-1	37.725	38.050	0.325	0.85%
S1-2	30.280	30.599	0.318	1.04%
S1-3	36.690	37.030	0.340	0.92%
S6-1	27.895	28.164	0.270	0.96%
S6-2	27.136	27.401	0.264	0.96%
S6-3	27.233	27.540	0.307	1.11%
S8-1	26.409	26.712	0.303	1.13%
S8-2	26.302	26.596	0.295	1.11%
S8-3	31.105	31.464	0.359	1.14%
S12-1	52.333	52.841	0.508	0.96%
S12-2	48.170	48.524	0.355	0.73%
S12-3	52.398	52.867	0.469	0.89%
S16-1	52.556	52.784	0.228	0.43%
S16-2	46.091	46.363	0.273	0.59%
S16-3	53.619	53.830	0.211	0.39%
S19-1	19.657	19.898	0.241	1.21%
S19-2	18.374	18.475	0.101	0.55%
S19-3	14.328	14.467	0.139	0.96%

Table 10 – Comparison between the total sediment discharge values (Qst) obtained in the NHSS computational tool and NH Sediment computation tool (Survey 2)

Measurement	Qst - NHSS [t.day-1]	Qst - WinTSR [t.day-1]	Qst - NH Sediment [t.day-1]	Difference between WinTSR and NHSS [%]	Difference between NH Sediment and NHSS [%]	Difference between WinTSR and NH Sediment [%]
C2-S19-3	14.33	14.29	14.47	-0.30%	0.96%	-1.28%
C2-S19-2	18.37	18.34	18.47	-0.17%	0.55%	-0.72%
C2-S19-1	19.66	19.58	19.90	-0.41%	1.21%	-1.63%
C2-S8-2	26.30	26.18	26.60	-0.45%	1.11%	-1.58%
C2-S8-1	26.41	26.29	26.71	-0.46%	1.13%	-1.62%
C2-S6-2	27.14	27.03	27.40	-0.40%	0.96%	-1.38%
C2-S6-3	27.23	27.11	27.54	-0.46%	1.11%	-1.59%
C2-S6-1	27.89	27.79	28.16	-0.39%	0.96%	-1.36%
C2-S1-2	30.28	30.16	30.60	-0.41%	1.04%	-1.47%
C2-S8-3	31.10	30.95	31.46	-0.49%	1.14%	-1.66%
C2-S1-3	36.69	36.56	37.03	-0.37%	0.92%	-1.30%
C2-S1-1	37.72	37.60	38.05	-0.34%	0.85%	-1.21%
C1-S20-3	38.17	38.09	38.40	-0.19%	0.61%	-0.81%
C1-S20-4	39.94	39.78	40.37	-0.38%	1.08%	-1.48%
C1-S20-2	43.66	43.52	44.05	-0.32%	0.88%	-1.21%
C2-S16-2	46.09	46.14	46.36	0.10%	0.59%	-0.49%
C1-S16-4	47.51	47.46	47.73	-0.12%	0.46%	-0.59%
C1-S20-1	47.58	47.47	47.88	-0.22%	0.65%	-0.87%
C2-S12-2	48.17	48.04	48.52	-0.26%	0.73%	-1.00%
C2-S12-1	52.33	52.15	52.84	-0.36%	0.96%	-1.33%
C2-S12-3	52.40	52.23	52.87	-0.32%	0.89%	-1.22%
C2-S16-1	52.56	52.59	52.78	0.07%	0.43%	-0.36%
C2-S16-3	53.62	53.65	53.83	0.06%	0.39%	-0.33%
C1-S12-4	65.43	65.24	65.95	-0.29%	0.80%	-1.09%
C1-S12-2	71.65	71.45	72.18	-0.27%	0.74%	-1.02%
C1-S12-3	78.07	77.86	78.65	-0.27%	0.73%	-1.00%
C1-S12-1	87.00	86.76	87.64	-0.28%	0.73%	-1.01%
C1-S8-2	88.20	87.93	88.84	-0.30%	0.73%	-1.03%
C1-S8-4	91.59	91.22	92.29	-0.41%	0.76%	-1.18%
C1-S8-3	92.03	91.72	92.76	-0.34%	0.79%	-1.13%
C1-S6-4	105.91	105.54	106.70	-0.35%	0.74%	-1.10%
C1/S6-1	107.42	106.98	108.31	-0.41%	0.82%	-1.24%
C1/S6-2	108.36	107.96	109.20	-0.37%	0.77%	-1.15%
C1/S1-3	113.00	112.73	113.65	-0.24%	0.58%	-0.82%
C1/S1-2	114.05	113.77	114.72	-0.25%	0.59%	-0.84%
C1/S1-4	116.87	116.56	117.61	-0.27%	0.62%	-0.90%
C1-S6-3	118.04	117.58	118.98	-0.39%	0.78%	-1.19%
C1/S1-1	126.80	126.47	127.58	-0.26%	0.61%	-0.88%

4 Concluding Remarks

The results of total solid discharge obtained with the developed computational tool characterize the transportation of sediments in water bodies and allow the identification of deposition spots and temporal variations in the sediment discharge.

In addition, the NH Statistic and Sediment computational tool achieves results consistent with other software and it can be said that, besides being reliable, it has a user-friendly interface and presents an user manual for all the tests and methods implemented, which makes its use simple and practical.

All in all, it is also important to note that the methodology used in the case study can be replicated to other sites, providing better information for the management and planning of water resources.

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